

# Optical Quantum Information Processing

P. Kwiat

An inaccurate history

An incomplete progress report

An unbiased vision...not

Anti-Outline

- Continuous-variable systems
- Atom-photon systems (cf. Kimble)
- Hybrid systems (cf. Lukin)
- Quantum imaging, or not
- ...

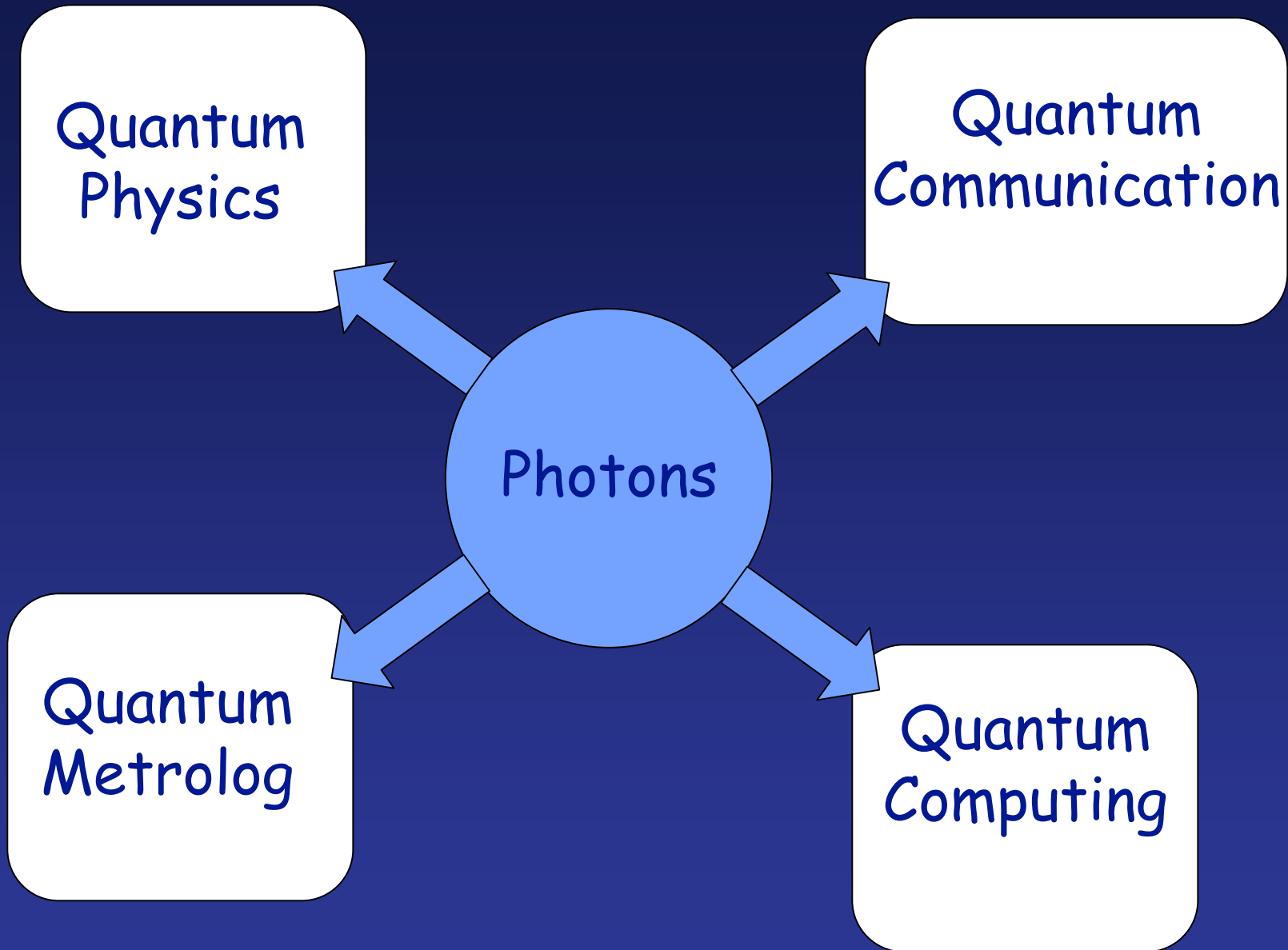
Quantum  
Physics

Quantum  
Communication

Photons

Quantum  
Metrolog

Quantum  
Computing

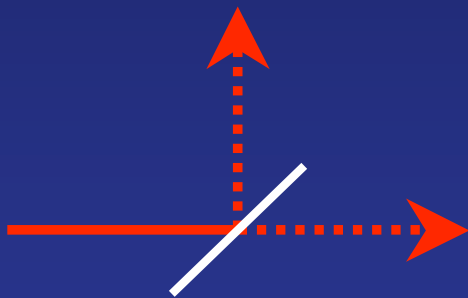




1905: Einstein proposed that light was really particles (for which he got the Nobel prize!)

How do you prove it?

The Beamsplitter...



Photon only detected in one output.

-use  $g^{(2)} = 0$  to test sources...

Equally likely to be transmitted or reflected -- cannot tell which:

-quantum random number generator (patented)

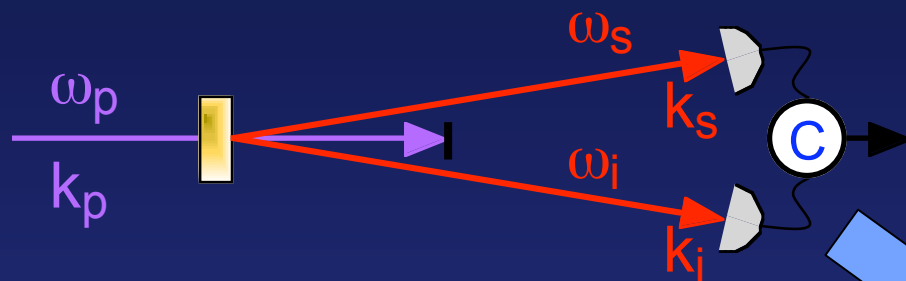
# Resources for Photonic Quantum Information Processing

## *Photon, but just 1:*

- Single emitter
  - atom/ion (Kimble) [hard to collect]
  - quantum dot ("designer atom")  
[BUT no two exactly alike...]
- Pair sources (SPDC, 4-wave mixing)
  - detection of signal photon -->  
"heralds" presence of idler photon  
in well-defined mode



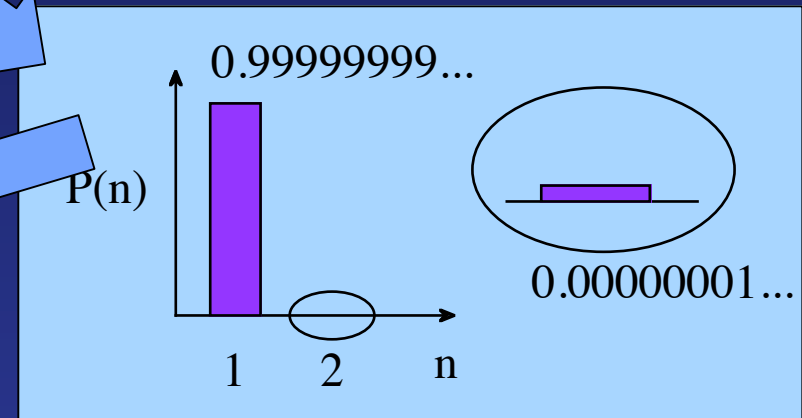
# Resources for Photonic Quantum Information Processing



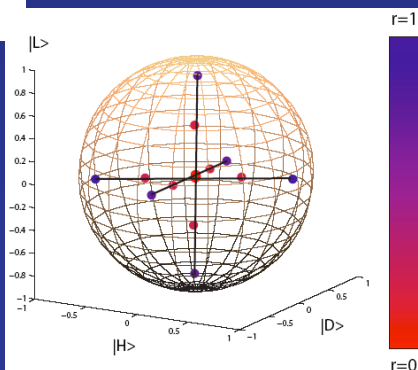
Spontaneous Parametric Downconversion

High-quality OTS components  $\Rightarrow$  >99.9% fidelity 'gates'

Well-behaved spatial modes



Conditional 1-photon per mode



***NOT "on-demand"***  
***(multiplexed sources help)***

# Resources for Photonic Quantum Information Processing

## *Detectors:*

- What we want
  - high efficiency (at  $\lambda$ ), low noise
  - fast (ideally at 100-fs scale)
  - photon-number resolving
- What we have now\*
  - APDs, VLPCs, TES, SSPDs
  - $\eta \sim 85\text{-}95\%$  (visible to 1550 nm)
  - 1 MHz - 1 GHz
  - can resolve up to  $\sim 10$  photons

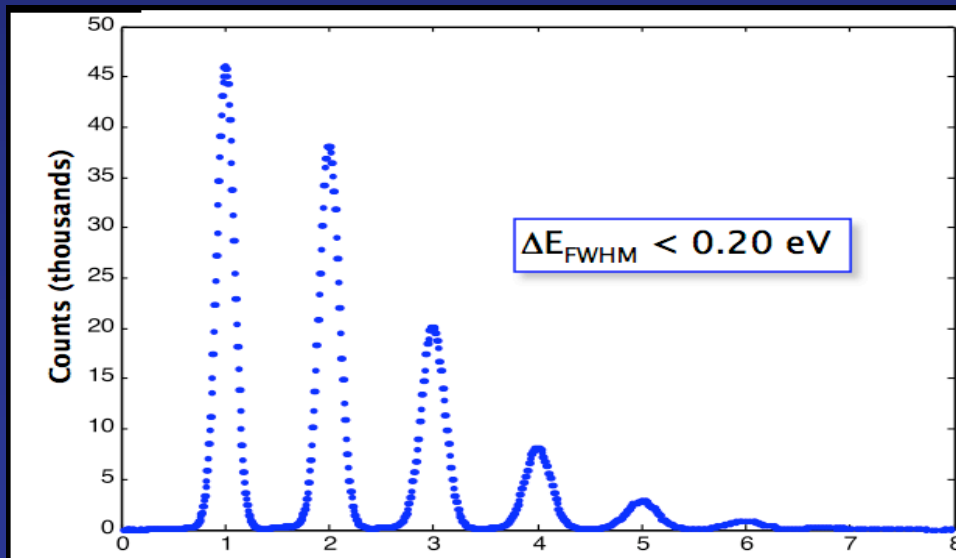
***\*But NOT all at once!***

# Resources for Photonic Quantum Information Processing

## *Superconducting bolometric detectors*

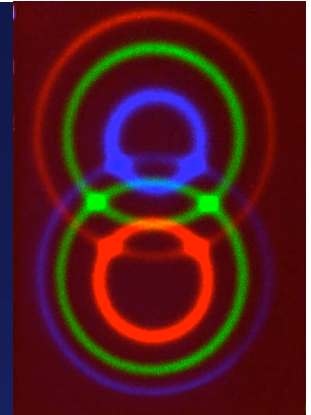


- system efficiency (at 1550 nm) ~95%  
(pushing toward 99%)
- near-perfect photon-number resolution
- slow-ish (0.1 - 1  $\mu$ s)

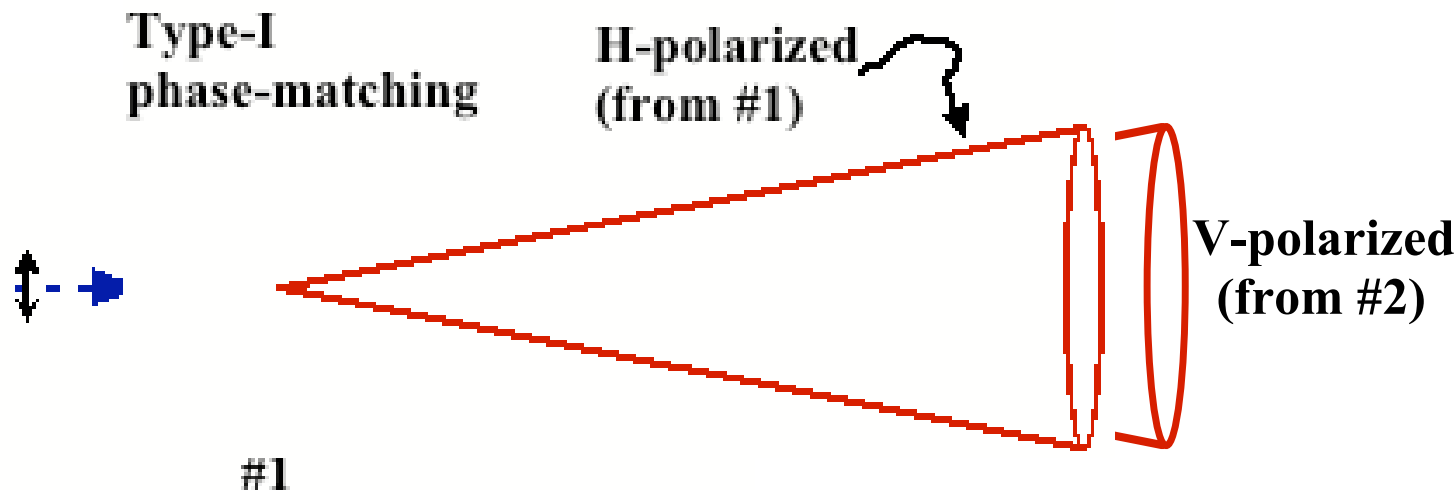


A.E. Lita, A. J. Miller, and  
S. W. Nam, Opt. Exp. 16,  
3032 (2008)

# (Polarization-) Entangled Source:

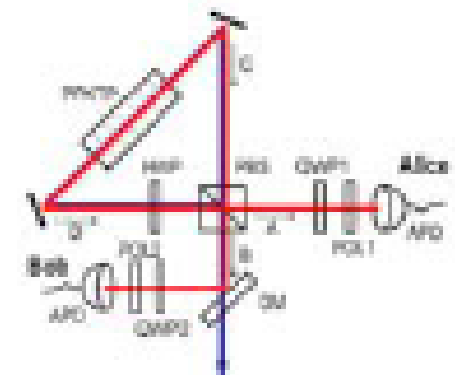


PRL 75,  
4337 (1995)



$$|\psi\rangle = \frac{1}{\sqrt{2}}(|H\rangle_1|H\rangle_2 + e^{i\varphi}|V\rangle_1|V\rangle_2)$$

Maximally entangled state



Tune pump polarization: → Nonmax. entangled, mixed states  
 Stable, simple → Used to test QM in various undergrad labs  
 New ultra-bright versions, narrow bandwidth, ...

**Not on-demand, unwanted entanglement in other DOFs**

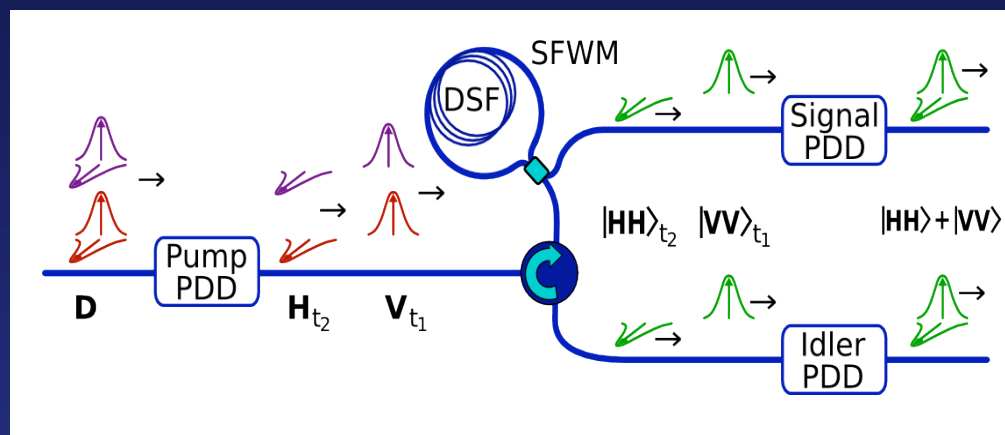
# Fiber-Based Sources (4-wave mixing)

@ NIST, Northwestern,...

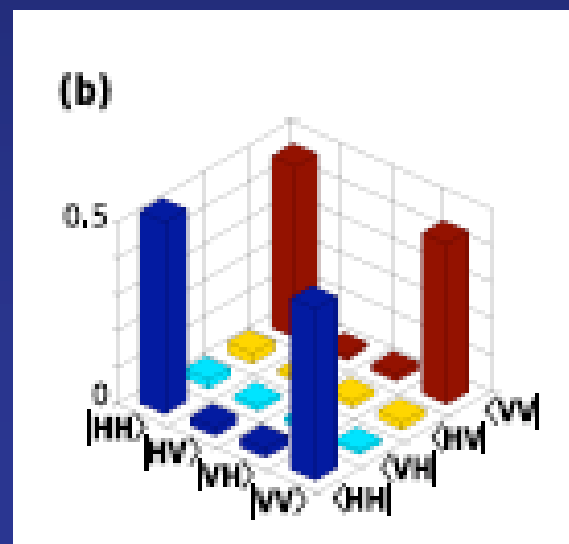
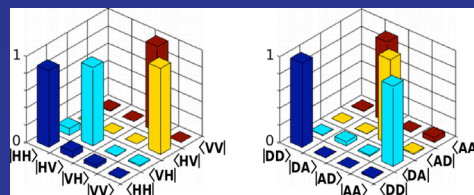
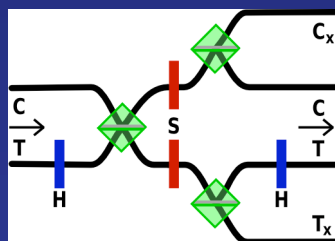
Degenerate Entanglement

Medic, et al. *CLEO Conference 2009*, paper ITuE7.

- Pairs created in fiber  
i.e., naturally single-mode
- Low-loss
- Exploits existing telecom infrastructure
- 1550 nm or 1310 nm
- Require cryogenic cooling



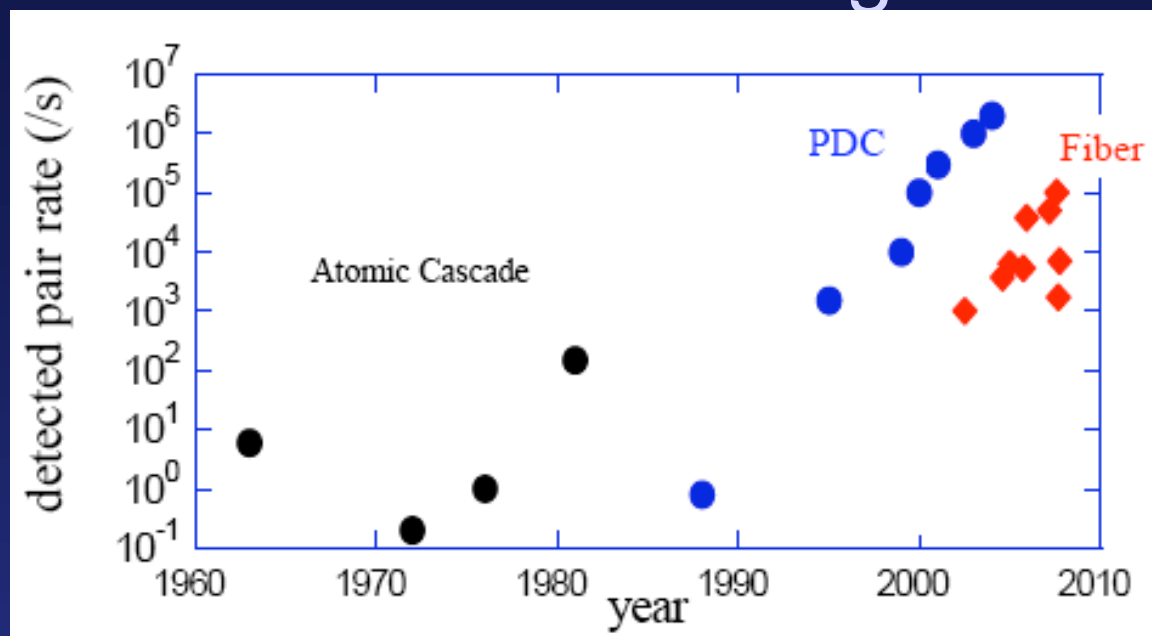
## LOQC Gates



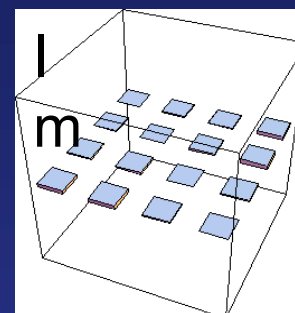
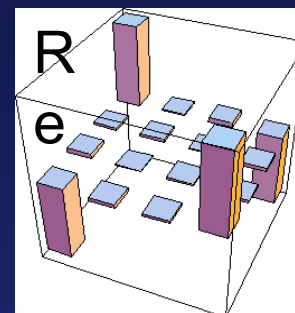
$F = 96\%$

Chen, et al. *Phys. Rev. Lett.* **100**, 133603 (2008).

# Moore's law for entanglement



$$\Phi^{(-)} \sim |HH\rangle - |VV\rangle$$



$F > 99.5\%$

**Polarization-entangled pairs @ 2,000,000 s<sup>-1</sup>,  
with  $F \sim 98\%$ ,  $T > 96\%$  Opt. Exp. 13, 8951 (2005)**

**Next main limitation: detector saturation**

## Bell-Ineq. Tests

$$S_{\text{LHV}} \leq 2 \quad |S_{\text{expt}}| = 2.7260 \pm 0.0008$$

(216 $\sigma$  in 0.8 s)

Optimized  $|S_{\text{QM, max}}| = 2\sqrt{2} = 2.828$

Bell test:  $|S_{\text{expt}}| = 2.826 \pm 0.005 \quad 165\sigma$

Now: Various tests  
with 2-5 photons  
(GHZ), with  
different DOFs,  
"qudits", etc.  
**More to come...**

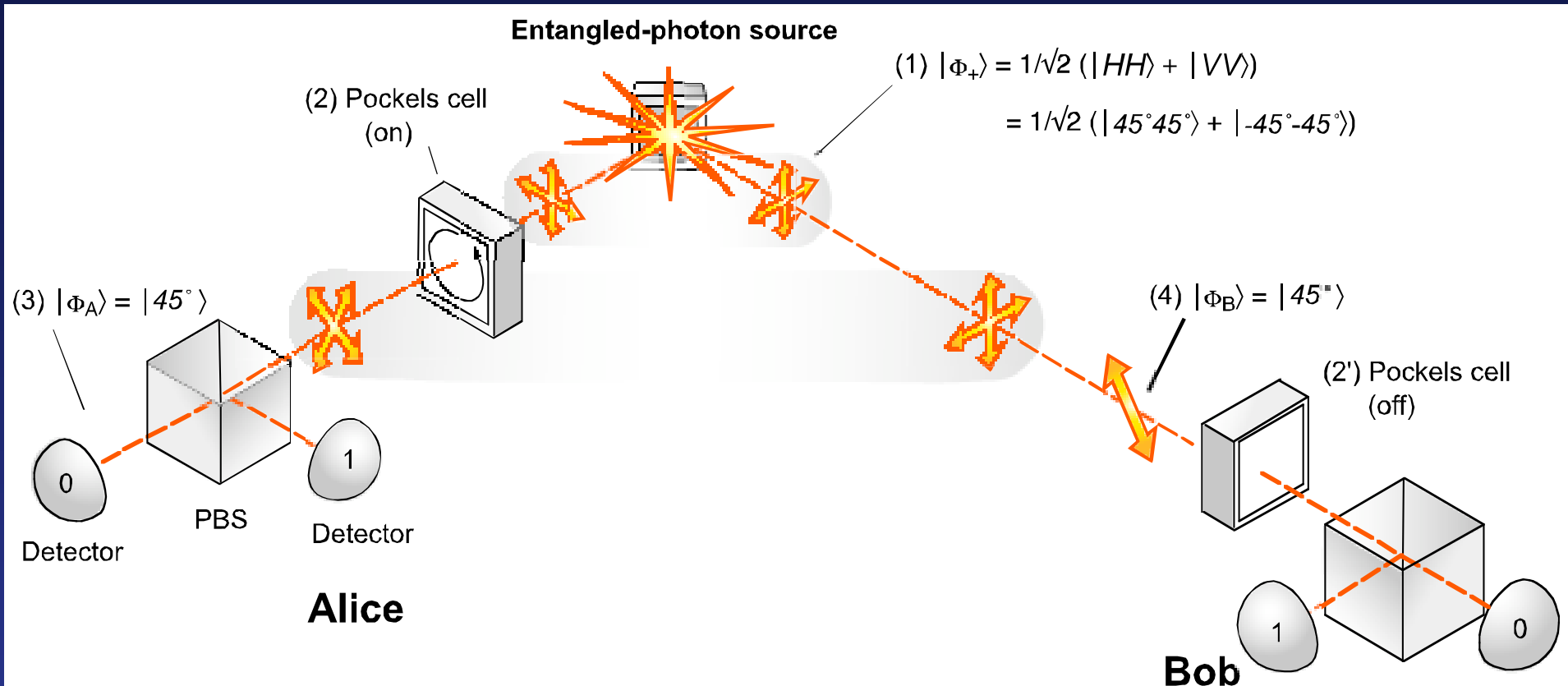


# on (and QKD) over 144-km and Tenerife (QIPS)



R. Ursin, et al. Nat.  
Phys. 3, 481 (2007)

# Entangled-Photon Quantum Cryptography



- Alice & Bob randomly measure polarization in the (HV) or the (45 -45) basis.
- Discuss via a “public channel” which bases they used, *but not the results*.
- Discard cases (50%) where they used different bases → uncorrelated results.
- Keep cases where they used the same basis → *perfectly correlated results!*
- Define  $H \equiv “0” \equiv 45$ ,  $V \equiv “1” \equiv -45$ . **They now share a secret key.**



# Entanglement Advantages for QKD

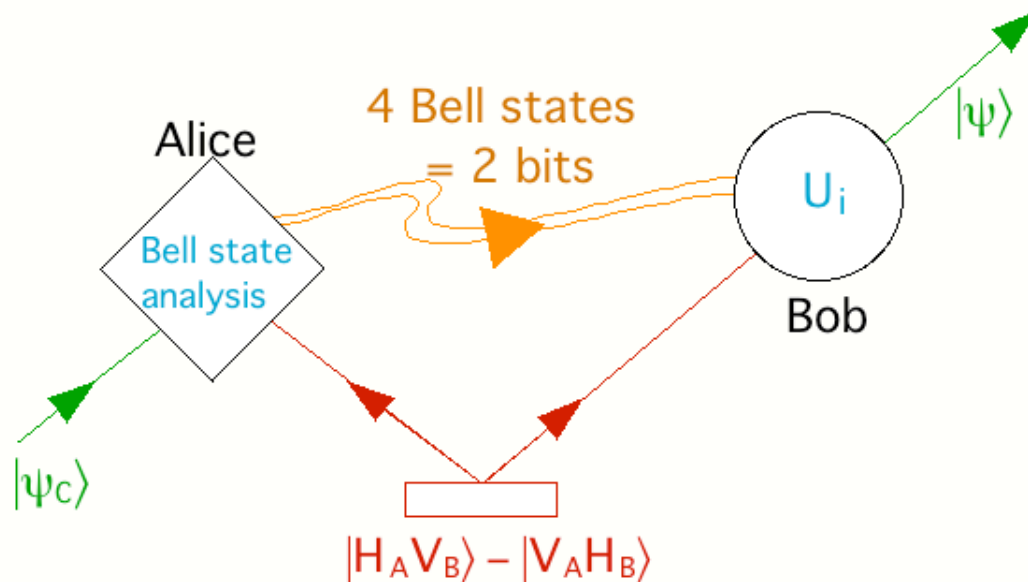
- Automatic randomness of key
- Longer distances accessible (since Bob knows *when* to look for a photon) [But decoy states...]
- Established methods to verify security of key
- Source can be automatically verified (even if “sold” by Evesdropper!)
- “Monogamy of entanglement”:  
Any leakage of info to other DOF  
⇒ increased bit error rate (BER)

Challenges: Source brightness/robustness to compete, e.g., with Decoy-state QKD. Fast quantum repeaters for long distance key distribution.

# Quantum Teleportation [Bennett *et al. Phys. Rev. Lett.* **70**, 1895 (1993)]

The basic idea → transfer the (infinite) amount of information in a qubit from Alice to Bob without sending the qubit itself.

Requires Alice and Bob to share entanglement:



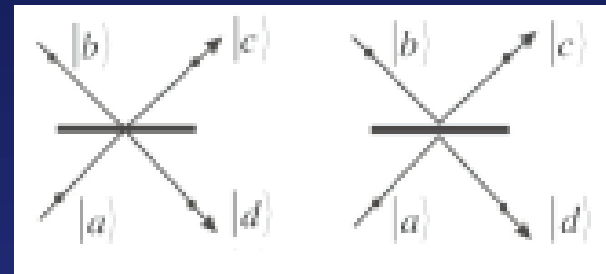
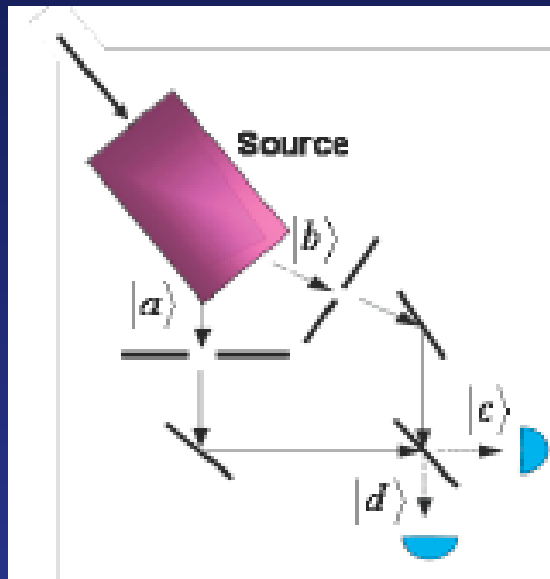
E.g. Alice measures photons C and A to be in a singlet state. Since C and A are orthogonal, and A and B are orthogonal, C and A must be *identical*!

## Remarks:

- The original state is gone.
- Neither Alice nor Bob know what it was.
- Requires classical communication – no superluminal signaling.
- **Bell state analysis is hard...**

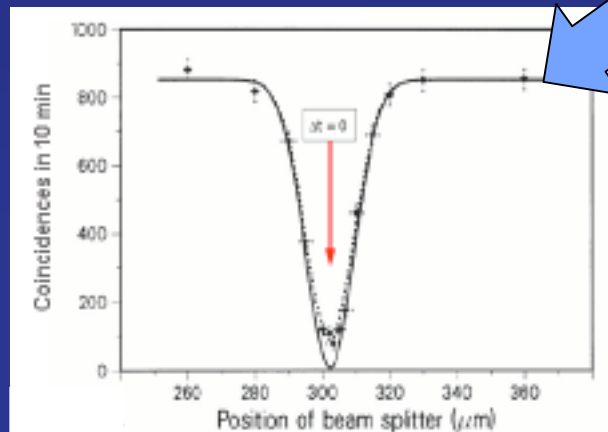
# Two-Photon Interference

*Traditional Hong-Ou-Mandel: interfere two photons (from same source):*



$$\left| \frac{1}{\sqrt{2}} \frac{1}{\sqrt{2}} + \frac{i}{\sqrt{2}} \frac{i}{\sqrt{2}} \right|^2 = 0$$

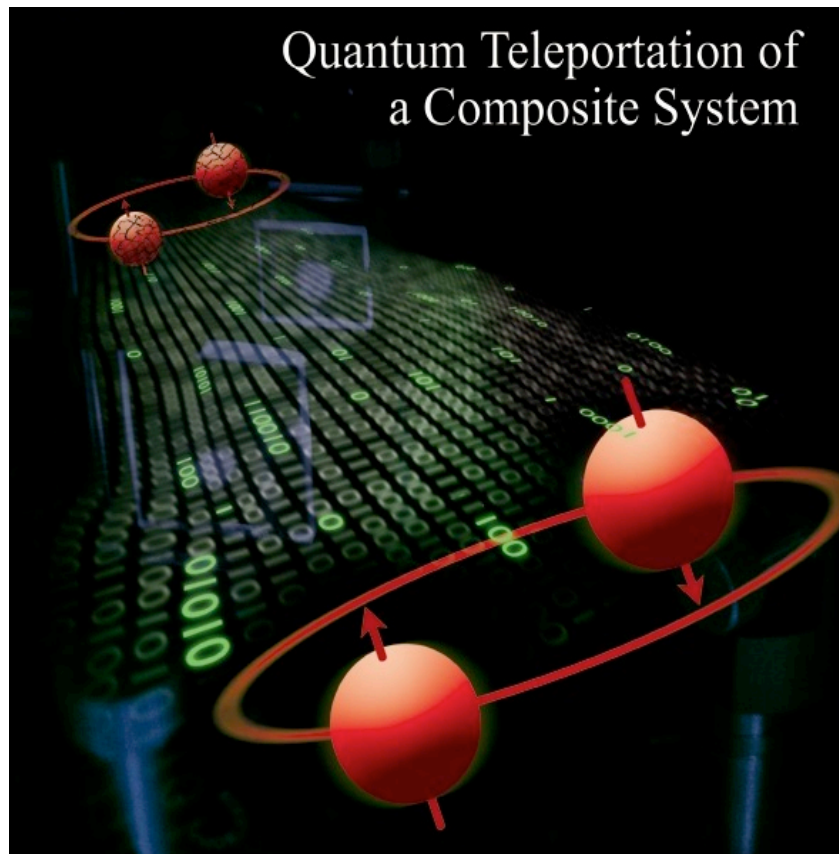
*Coincidence Probability*



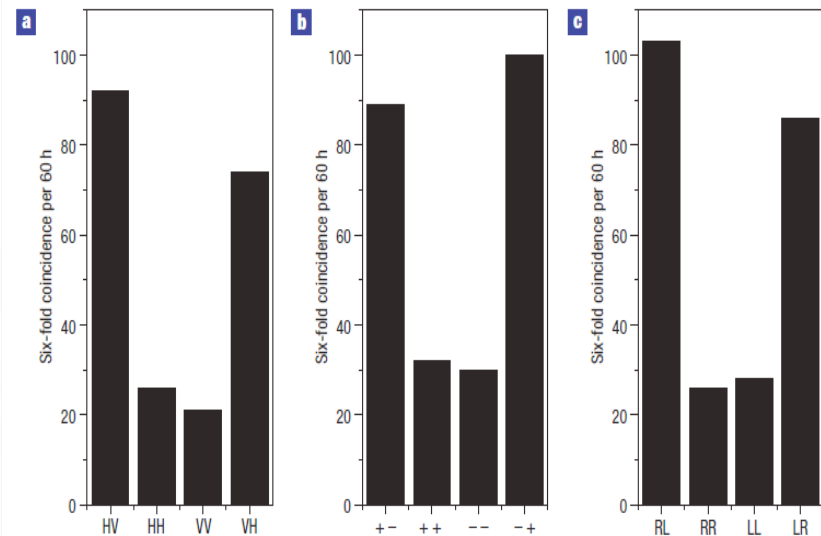
*Photons must be indistinguishable (& not entangled to other photons)!*

# Experimental Teleportation

Bouwmeester et al., Nature 390, 575 (1997)



## Experimental results of teleporting an entanglement



**But very low rate -- 6-photon experiment: 100/60 hours**

Q. Zhang et al. Nature Physics 2, 678 (2006)

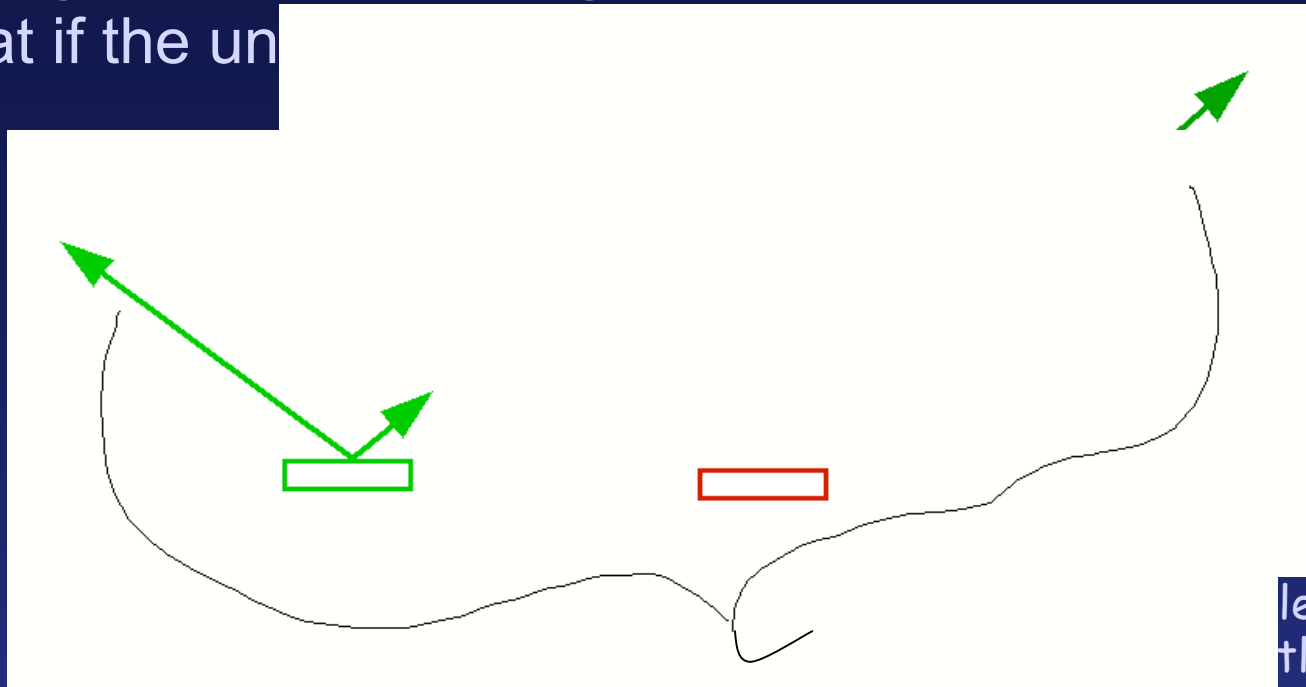
N states of ions, other degrees of freedom, 2-qubits, entanglement,...

What are the limits? How large (complex) of a system?  
How far? How fast? Teleport complex "process"?

# Entanglement Swapping

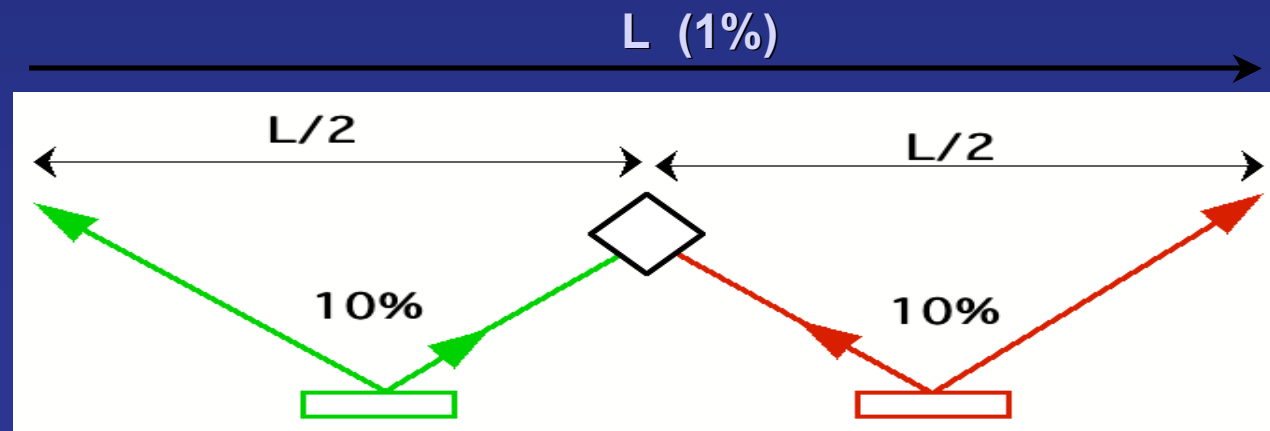
What if the un

a 4th particle?



led, despite that  
tly interacted!

**Need to distribute entanglement over longer distances (repeaters):**



Need ~100 pairs

Need ~20 pairs

If we have a **quantum storage device** we can wait until we have a pair from both sides.

# Photon Entanglements

- **Polarization (spin)**  
(Ou & Mandel, Shih & Alley, etc., etc.)
- **Linear momentum**  
(Rarity & Tapster)
- **Orbital angular momentum**  
(Zeilinger et al.)
- **Time-Bin**  
(Gisin et al., Inoue et al.)
- **Energy-Time**  
(Franson et al., Howell et al.)
- **3,4,5, high photon number** (many)

# Hyper-Entanglement

PGK, JMO 44, 2173 (1997)

- Photons simultaneously entangled in multiple DOFs:

$$\underbrace{(|H, H\rangle + |V, V\rangle)}_{\text{polarization}} \otimes \underbrace{(|rl\rangle + \alpha|gg\rangle + |lr\rangle)}_{\text{spatial modes}} \otimes \underbrace{\int_0^{E_p} dE A(E) |E\rangle_s |E_p - E\rangle_i}_{\text{energy}}$$

- Enlarged Hilbert space:  $2 \otimes 2 \otimes m \otimes m \otimes n \otimes n$
- Easy to perform quantum logic *between* DOFs
- More efficient n-qubit transfer:  $T$  vs  $T^n$
- New capabilities in quantum info. processing
  - full Bell-state analysis
  - “super-duper” dense coding
  - quantum communication with higher alphabets
  - remote preparation of entangled states
  - ???

# Quantum “superdents coating”

## PHYSICAL REVIEW LETTERS

VOLUME 69

16 NOVEMBER 1992

NUMBER 20

### Communication via One- and Two-Particle Operators on Einstein-Podolsky-Rosen States

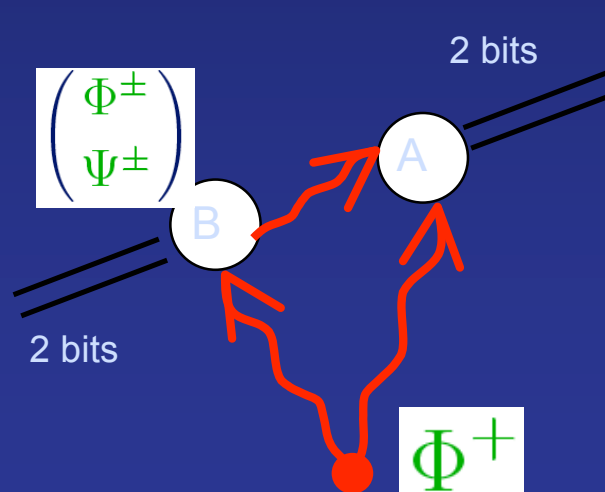
Charles H. Bennett

*IBM Research Division, T. J. Watson Research Center, Yorktown Heights, New York 10598*

Stephen J. Wiesner

*74 Parkman Street, Brookline, Massachusetts 02146*

(Received 16 June 1992)



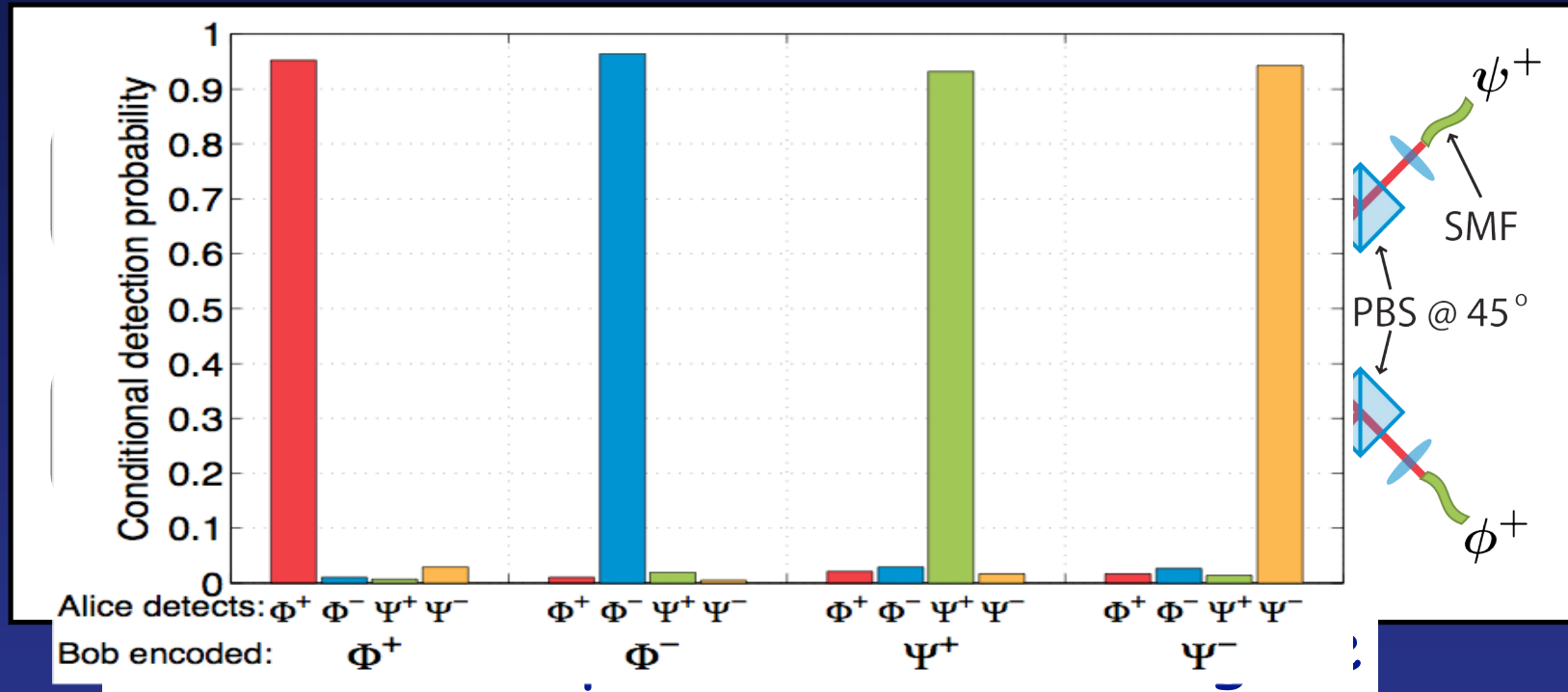
- ✓ 1 entangled photon each to Bob and Alice
- ✓ Bob applies one of 4 U's  $\Rightarrow$  1 of 4 Bell states; sends photon to Alice
- ✓ Alice: BSA  $\Rightarrow$  infer one of 4 messages

Channel cap. =  $\log_2 4$   
= 2bits/photon\_from\_Bob

Full BSA analysis  
“impossible” with  
linear optics...



# Hyperentanglement-enhanced Superdense Coding



Average success probability: 95%  
 $\Rightarrow$  channel capacity:  $1.630(6) > 1.58$   
 ("limit" for linear optics superdense coding, i.e., without hyperentanglement)

Barreiro et al., Nature Physics 4, 282 (2008)

What are the limits?  
 How many bits/photon?  
 Can the "hitchhiker" qubits be used, e.g., for error correction?

# Why Optical Quantum Computing?

“Photons been very very good to me”

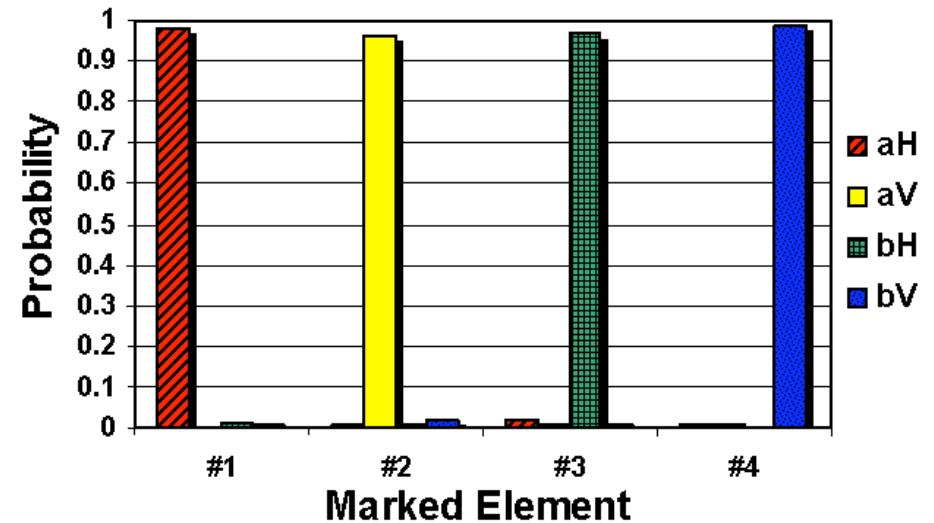
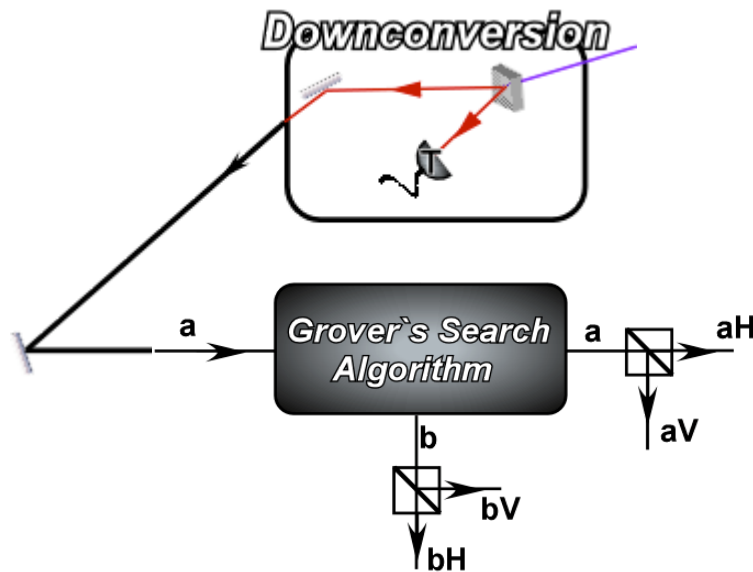
- Very little/no decoherence -- photon's don't interact
- Excellent performance with off-the-shelf optics
- Very fast gates: single-qubit  $\sim 10$  ps - 5 ns  
two-qubit  $< 150$  ns

# Why *not* Optical Quantum Computing?

- Photon's don't interact -- 2-qubit gates hard
- Linear approach: measurement-induced nonlinearity
- Nonlinear approach: Zeno and QND gates

# Grover's search algorithm with linear optics

Optical realization with single photons: A database of four elements



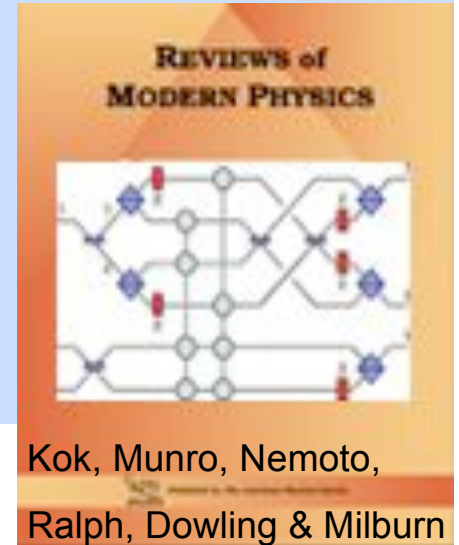
Accuracy: ~97.5% (as of 2004)

- Gates: Linear optical elements
- Nonscalable -- each new qubit doubles the required number of optical elements

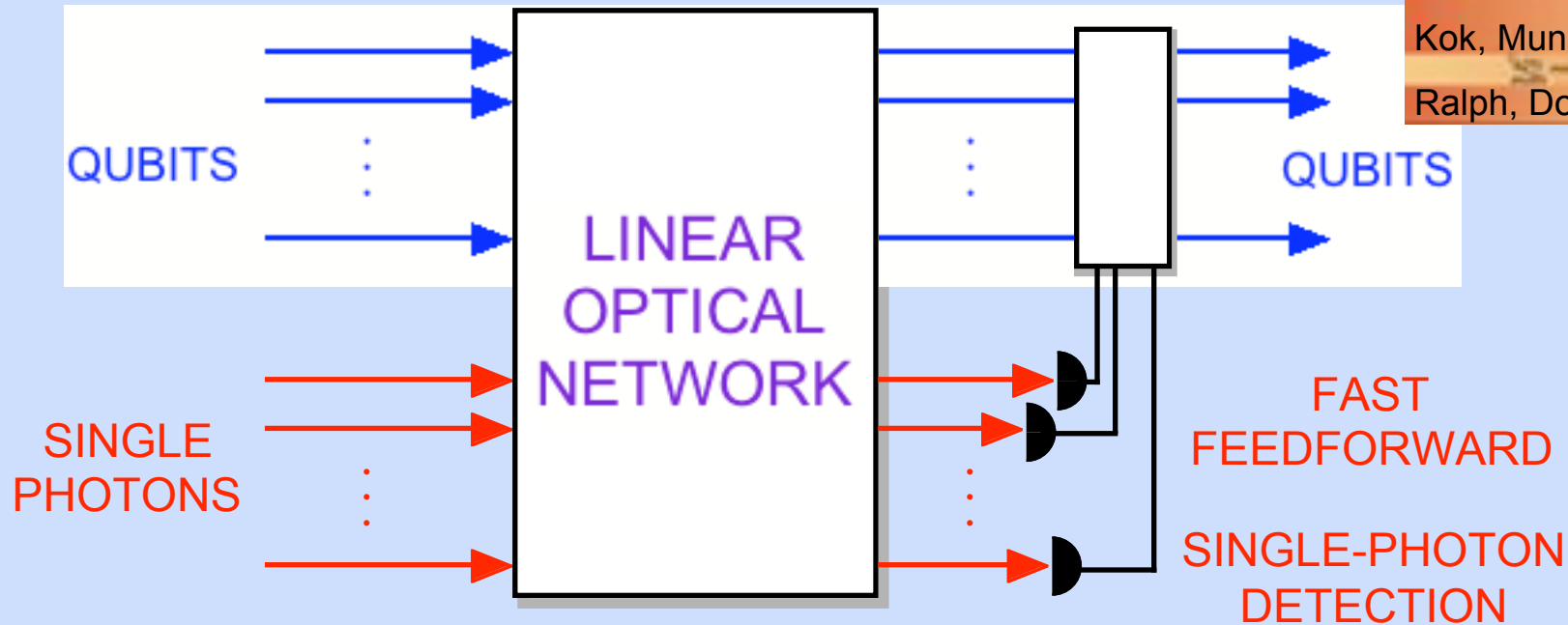
# Linear optical quantum computing



Knill, Laflamme and Milburn,  
*Nature* **409**, 46 (2001)



Kok, Munro, Nemoto,  
Ralph, Dowling & Milburn

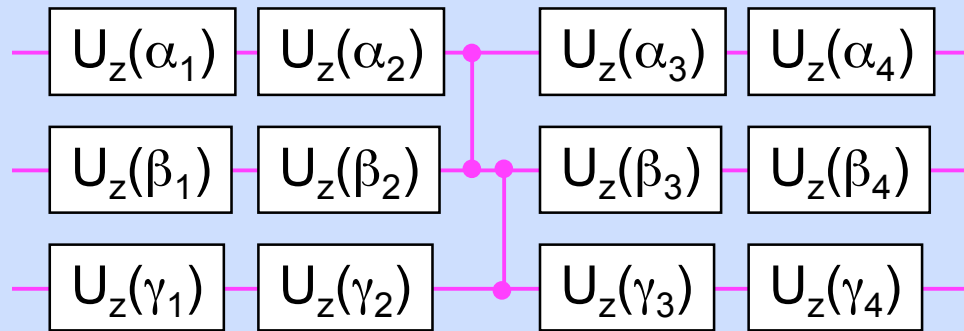


**LARGE overhead requirements...(>10<sup>5</sup>/gate)**

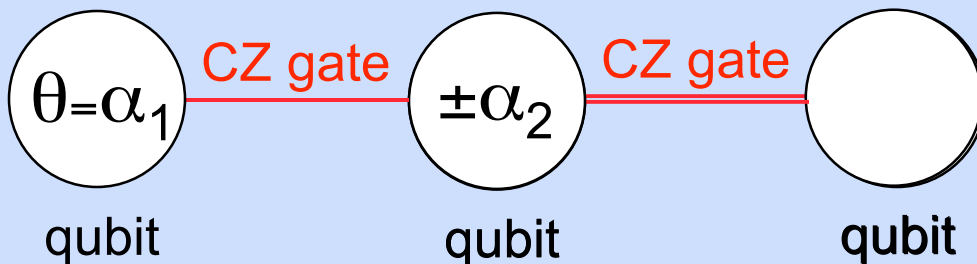
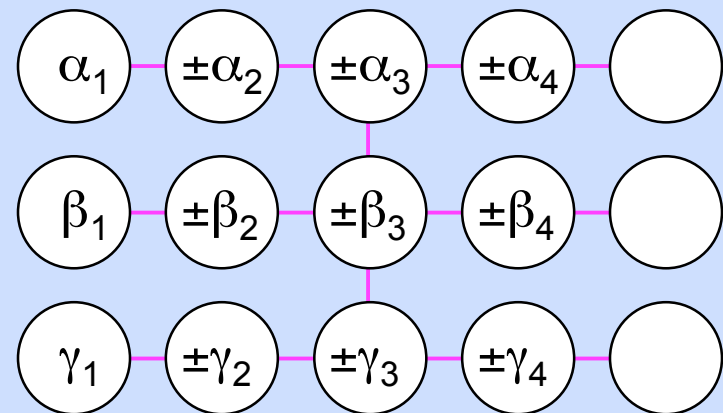
# A New Paradigm: Measurement-based computation

- 2004 - Nielsen's solution: combine KLM non-deterministic gate with cluster-state model of quantum computation

conventional circuit



cluster circuit



Measurement on qubits  
 $\cos(\theta)\sigma_x + \sin(\theta)\sigma_y$

Photons are hard to hold, but with cluster states you can build as you go...

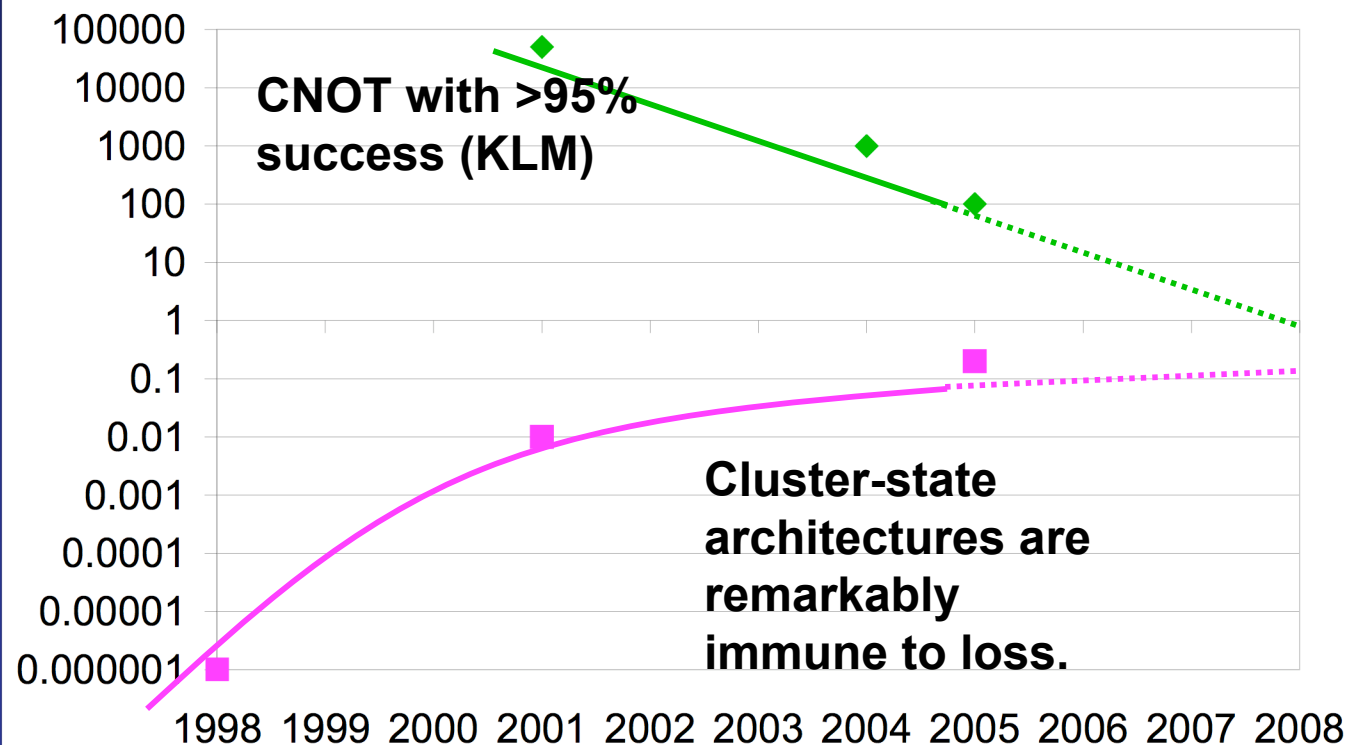


## Optical quantum computing OQC Anti-Moore's Law

Graph states (clusters and parity-encoding techniques) have greatly reduced the required resources and the loss-tolerance threshold for LOQC:

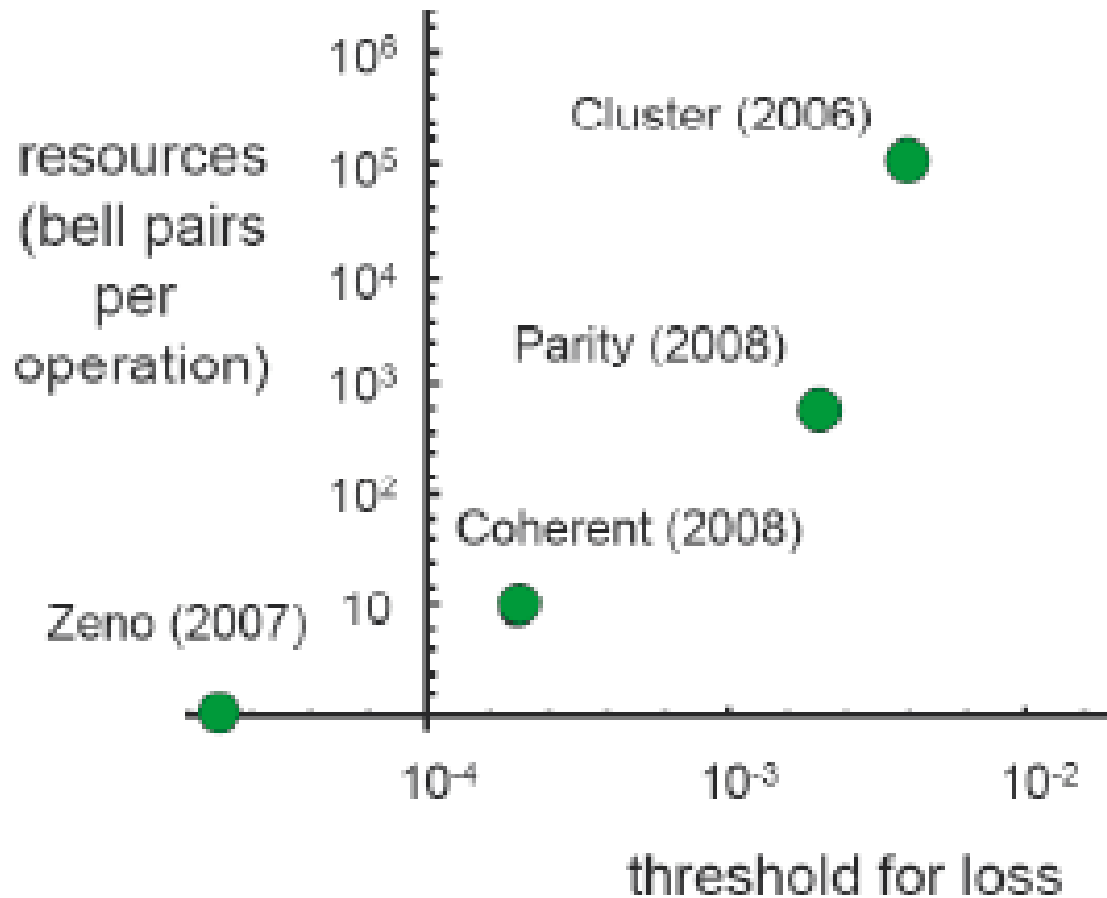
Resources (Bell states, operations, etc.) for a reliable entangling gate

Acceptable loss for a scalable architecture



Efficient LOQC possible if (source purity) × (detection effic.) > 2/3.

# The tradeoffs between Resources and Loss-threshold

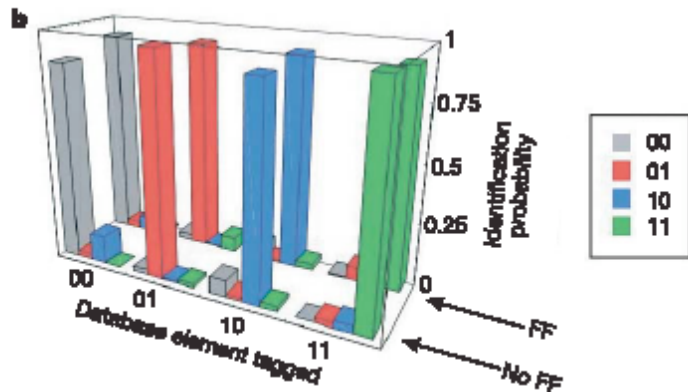
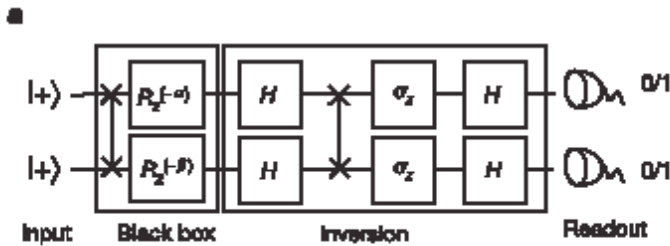
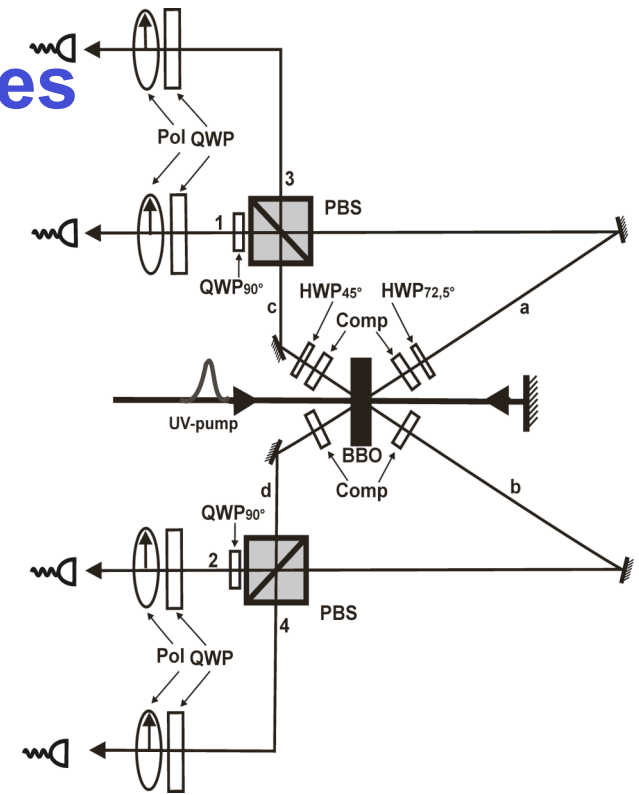




## ➤ Realization of photon cluster states

- Direct creation via down-conversion
- Interferometric setup
- Simple polarizers

$$\frac{1}{2} \left( |H\rangle_1 |H\rangle_2 |H\rangle_3 |H\rangle_4 + |H\rangle_1 |H\rangle_2 |V\rangle_3 |V\rangle_4 \right. \\ \left. + |V\rangle_1 |V\rangle_2 |H\rangle_3 |H\rangle_4 - |V\rangle_1 |V\rangle_2 |V\rangle_3 |V\rangle_4 \right)$$



Grover search algorithm  
Walther et al., Nature **434**, 169 (2005)

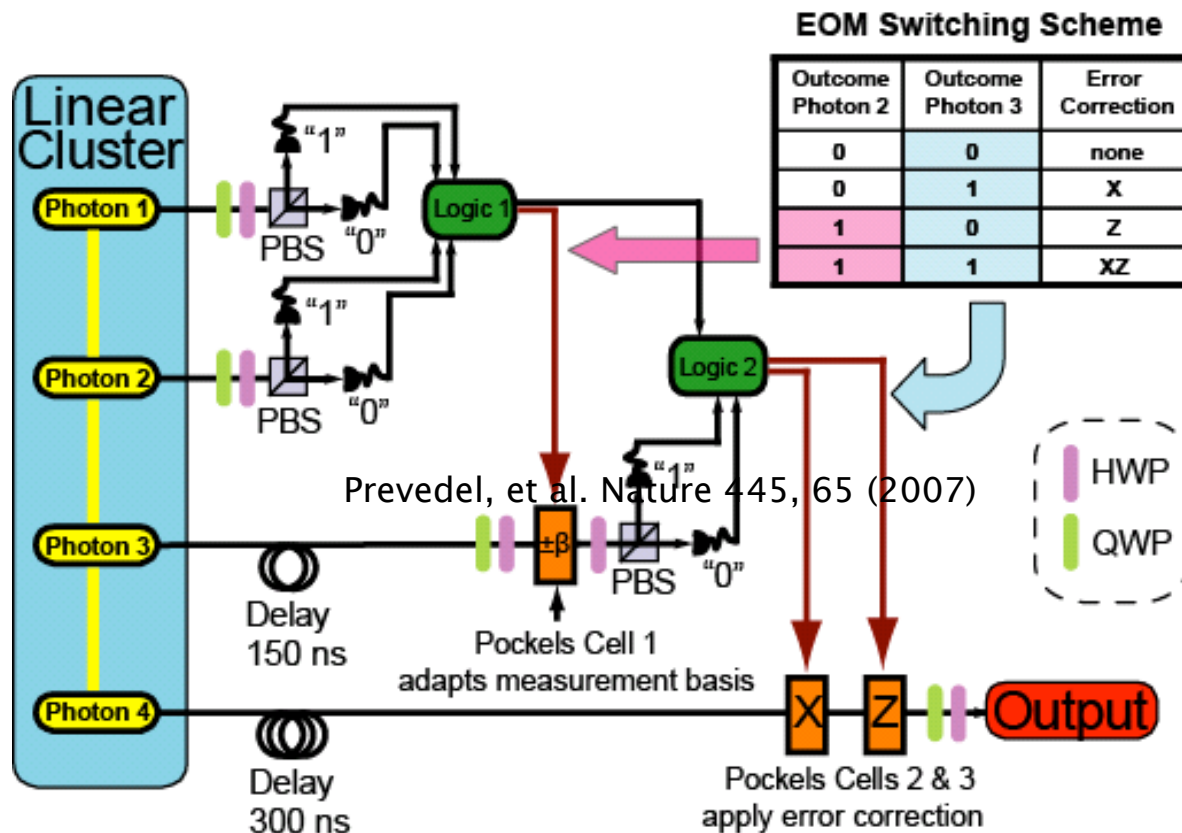
## ➤ Present status:

- 1-qubit gate fidelity:  $F > 90\%$
- Few count rates:  $10^{-1}$  3-pair/s
- Thus far up to  $n = 6$  (at very low rates)

Need 'on-demand' sources,  
better detectors, and better  
wires...

# Feed-Forward Implementation

Prevedel, et al. Nature 445, 65 (2007)



**Pockels Cells:**

KD\*P crystals ~ 6.3 kV

**Over 99 % fidelity (500:1)**

Fibers to detector 15ns  
 Detector-Delay 35ns  
 EOM-Delay 65ns  
 Logics-Delay 7.5ns  
 Misc. cables 20ns

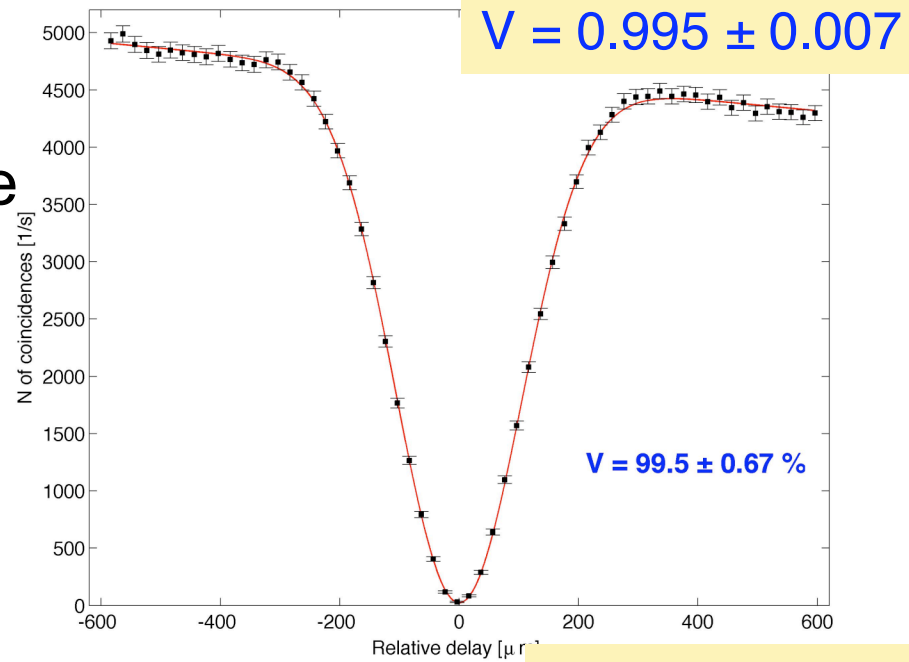
**Feed-Forward  
 Time < 150 ns !!**

**~1 ns possible  
 (w better  
 detectors,  
 integrated optics)**

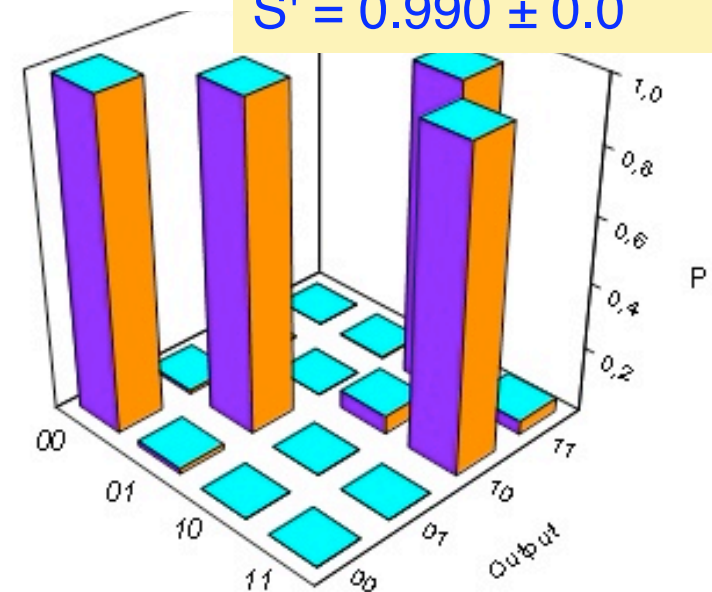
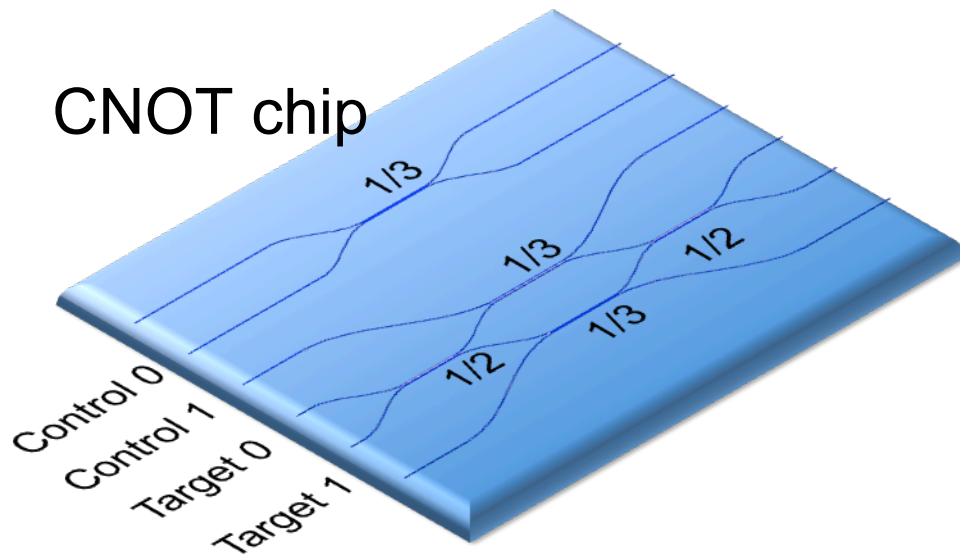
# Silica-on-silicon Quantum Photonics



Quantum  
interference



$$S' = 0.990 \pm 0.0$$

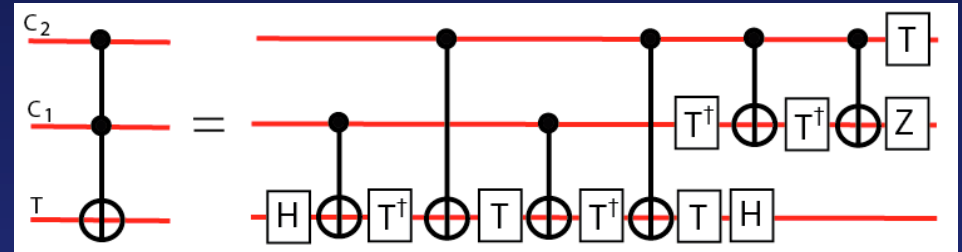


# Harnessing higher dimensions to reduce LOQC resources

- Even small quantum algorithms require large numbers of CU and Toffoli gates  
controlled-U gates: phase estimation, quantum chemistry..  
Toffoli gates: Shor's, error correction, fault tolerance...

- What if your architecture only has 2-qubit gates?

e.g., build Toffoli with 6 CNOT's



- Works by coherently isolating some quantum information from gate actions

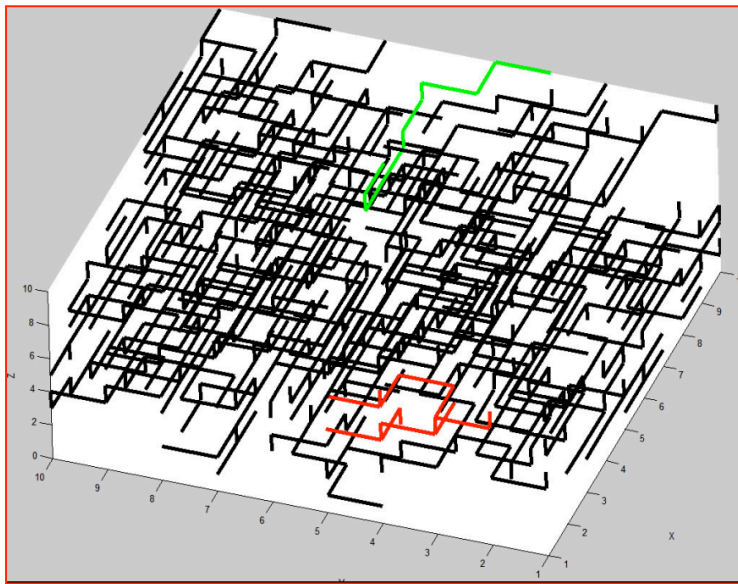
|                           | chained gates |            | new scheme   |            |  |
|---------------------------|---------------|------------|--------------|------------|--|
| no. photons               | 11            | 15         | 3            | 7          | practical<br>circuit<br>for<br>demonstrating<br>Toffoli Gate |
| probability<br>of success |               | 1/4096     | 1/72         | 1/32       |  |
|                           | min. photons  | max. prob. | min. photons | max. prob. |  |

1/2073  
6

**What are the limits, e.g., when going for fault-tolerance...?**

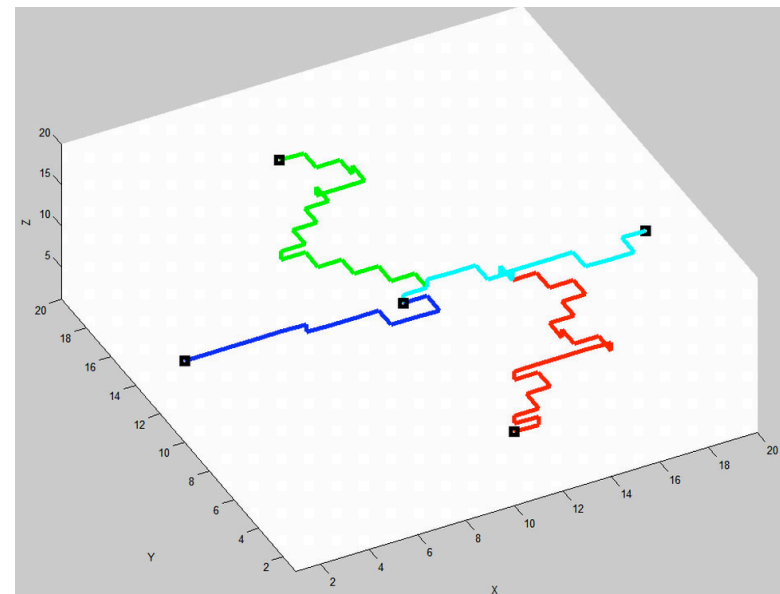
# How to brew Really BIG Cluster-states: Percolation

Fusion success probability =  $1/2$ ,  
above percolation threshold.  
 $\Rightarrow$  get large piece of connected  
cluster state with high probability



Red & Green – not connected  
Black – connected

From the percolated cluster it is easy to  
compute measurement patterns to  
produce any desired cluster circuit:



- Every photon undergoes only one Type-I gate and one single-qubit measurement
- Removes requirement for photon rerouting (only requires feedforward to classical measurement settings)
- Initial resources can be as small as 4-photon cluster states

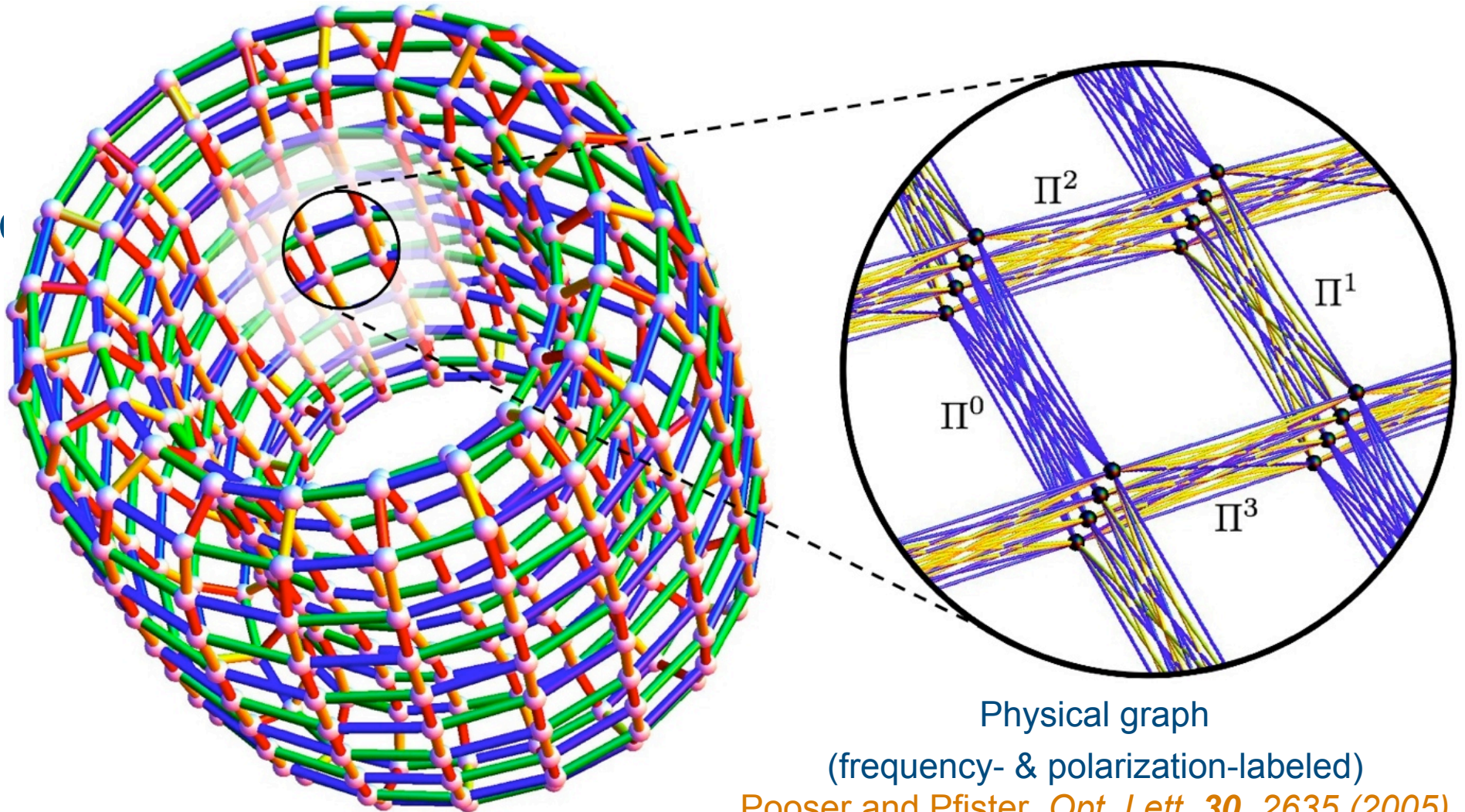


# Scalable quantum computing in the optical frequency comb

Menicucci, Flammia, and Pfister, *Phys. Rev. Lett.* **101**, 130501 (2008)

## Classical frequency comb

The eigenmodes of a cavity form a naturally scaled ensemble of classically coherent modes



Pooser and Pfister, *Opt. Lett.* **30**, 2635 (2005)

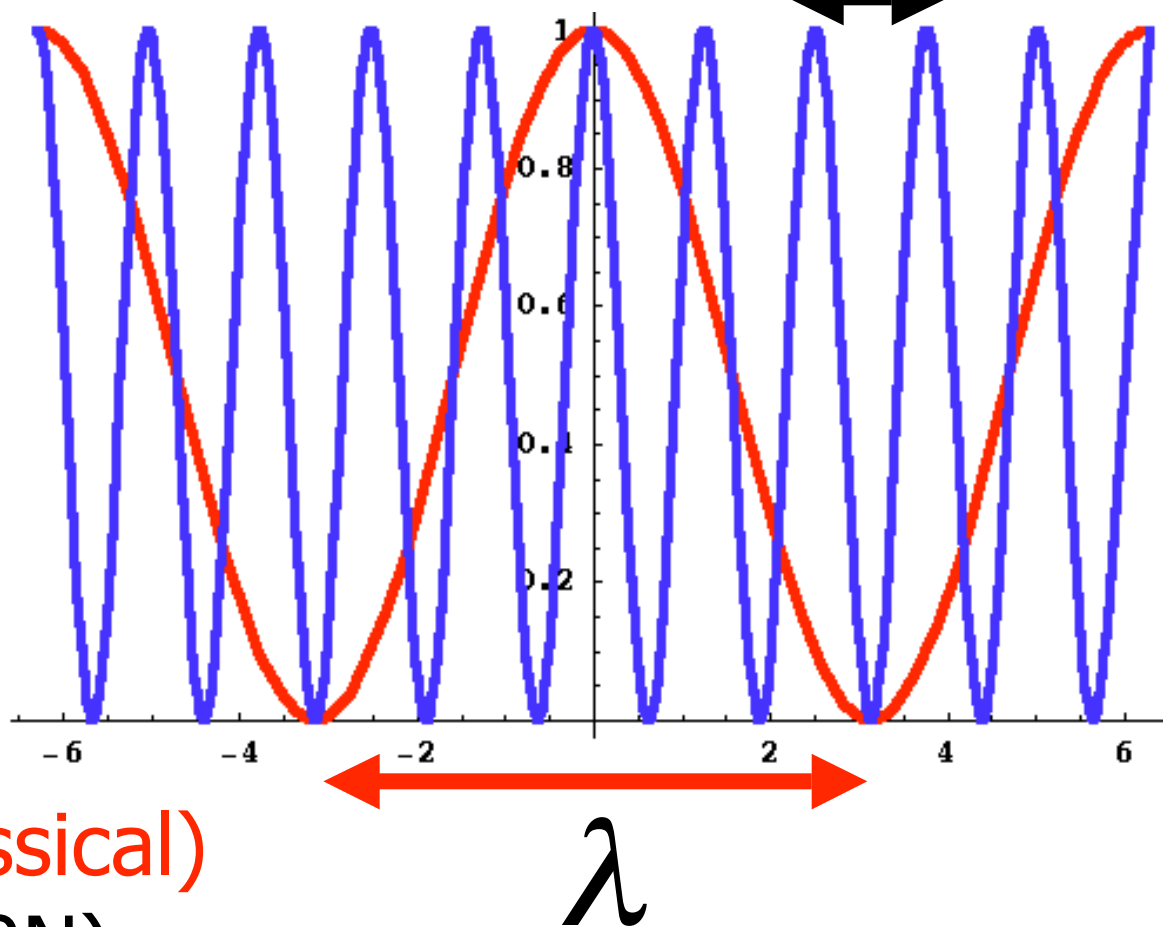


# Super-Resolution á la NOON



$$|N :: 0\rangle_{a,b} \equiv \frac{1}{\sqrt{2}} (|N, 0\rangle_{a,b} + |0, N\rangle_{a,b})$$

$$\lambda / N$$



N=1 (classical)

N=5 (NOON)

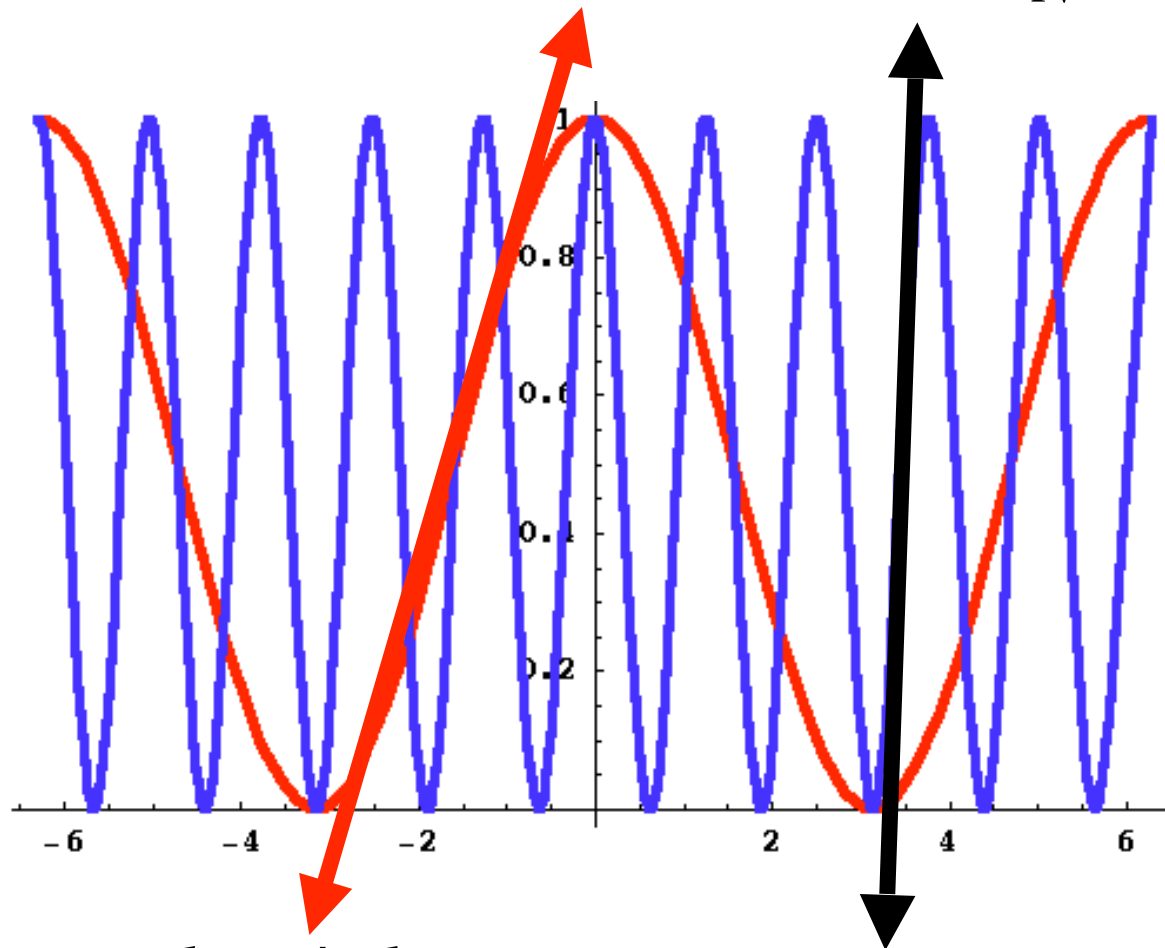


# $\Delta \hat{P}$ Super-Sensitivity

$$\Delta \varphi = \frac{\Delta \hat{P}}{\left| d \langle \hat{P} \rangle / d\varphi \right|}$$

$$dP_N / d\varphi$$

N=1 (classical)  
N=5 (NOON)



$$dP_1 / d\varphi$$

For Many Sensor Applications — LIGO, Gyro, etc., — We Don't CARE Which Fringe We're On!

The Question for Us is IF any Given Fringe Moves, With What Resolution Can We Tell This!?

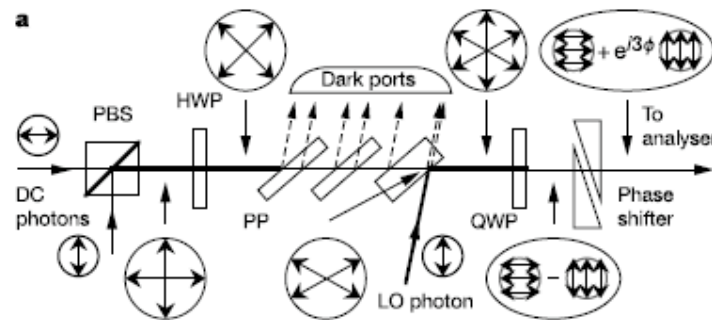
*How do we efficiently create these exotic states? What else are they good for?*



**1990**

2-photon

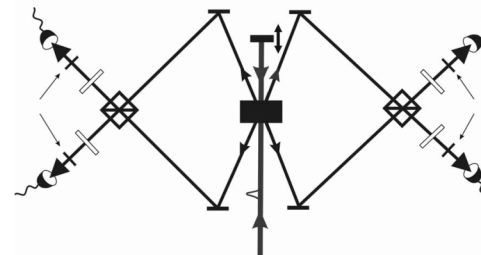
Rarity, (1990)  
Ou, et al. (1990)  
Shih, Alley (1990)  
....



Mitchell,...,Steinberg  
Nature (13 MAY)  
Toronto

**2004**

3, 4-photon  
Super-  
resolution



Walther,...,Zeilinger  
Nature (13 MAY)  
Vienna

**6-photon  
Super-Resolution**

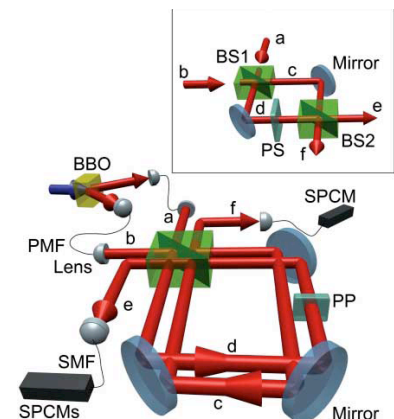
Resch,...,White  
PRL (2007)  
Queensland

**2007**

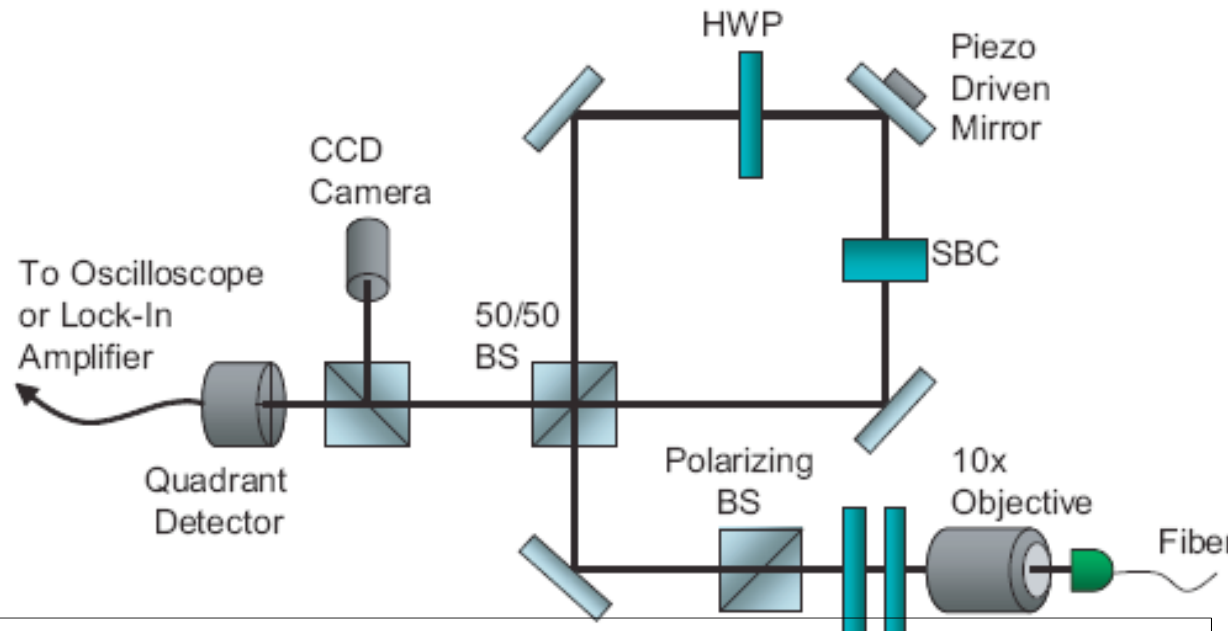
**4-photon**

Super-sensitivity  
&  
Super-resolution

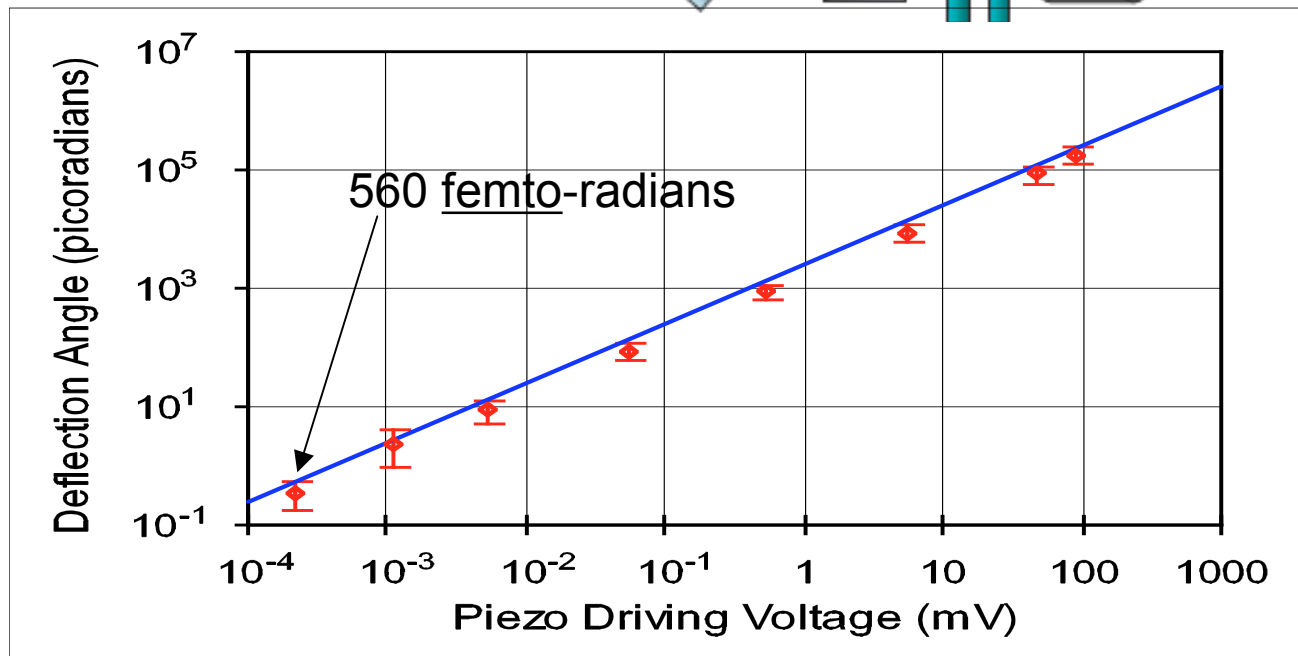
Nagata,...,Takeuchi,  
Science (04 MAY)  
Hokkaido & Bristol



# Weak-Value-Enhanced Deflection-Detection



J. Howell et al.,  
Phys. Rev.Lett.  
(In Press for April)



This is a *classical* enhancement, discovered by studying QM weak measurements. So what!

What are the limits when combined, e.g., with squeezed input light, or N00N states, or...?

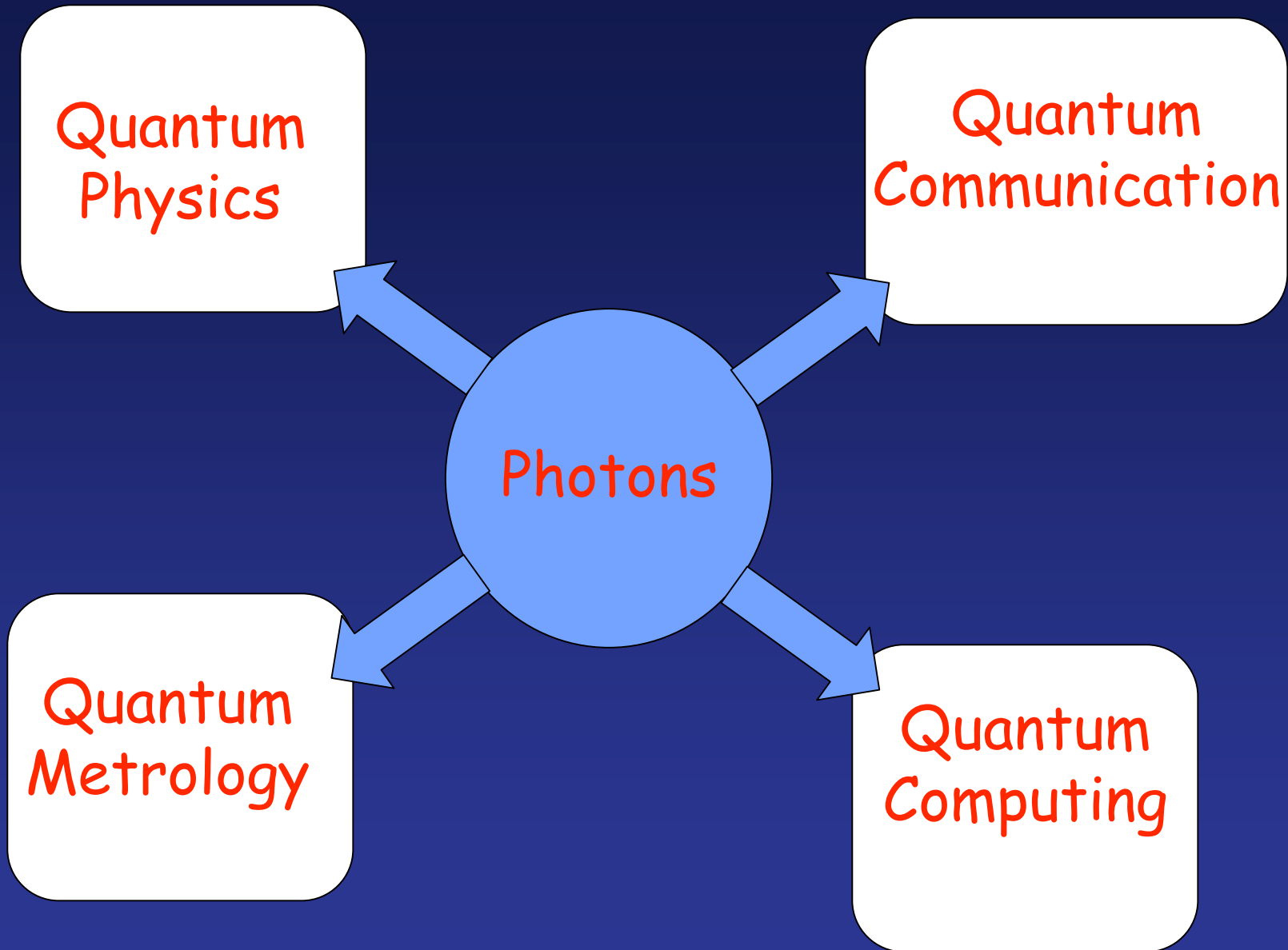
Quantum  
Physics

Quantum  
Communication

Photons

Quantum  
Metrology

Quantum  
Computing



# Quantum Battle Space of Tomorrow



**What good is  
Quantum  
Information for  
Video Games??**